

There's less here than meets the eye. He's not deriving much of anything; he's just finding the derivatives in the Greek coordinate system.

I'll work through the first equation he gives here. I haven't done the rest but I think they follow similarly. It's a mess, but all we're doing is applying the chain rule a few times and plugging in Maxwell's equations in the Latin frame in order to get the derivatives of the Latin (unprimed) functions X, Y, Z, L, N, M in terms of the Greek coordinates.

First we have the X component of the partial of the E field:

$$(1) \quad \frac{1}{c} \frac{\partial x}{\partial t} = \frac{\partial N}{\partial y} - \frac{\partial M}{\partial z}$$

And we'll need an equation Einstein didn't bother to write down right here, which is the divergence of the E field:

$$(2) \quad \begin{aligned} \frac{\partial X}{\partial x} + \frac{\partial Y}{\partial y} + \frac{\partial Z}{\partial z} &= 0 \\ \frac{\partial X}{\partial x} &= - \left[\frac{\partial Y}{\partial y} + \frac{\partial Z}{\partial z} \right] \end{aligned}$$

And we have the transforms between the Latin and Greek frames:

$$(3) \quad \begin{aligned} t &= \beta \left(\tau + \frac{v}{c} \xi \right) \\ x &= \beta \left(\xi + \frac{v}{c} \tau \right) \\ y &= \eta \\ z &= \zeta \end{aligned}$$

$$(4) \quad \begin{aligned} \tau &= \beta \left(t - \frac{v}{c} x \right) \\ \xi &= \beta \left(x - \frac{v}{c} t \right) \end{aligned}$$

Now let's write the partial derivative of X with respect to tau (this has nothing to do with Maxwell's equations; this would be true for any function X):

$$(5) \quad \frac{\partial X}{\partial \tau} = \frac{\partial X}{\partial t} \frac{\partial t}{\partial \tau} + \frac{\partial X}{\partial x} \frac{\partial x}{\partial \tau} + \frac{\partial X}{\partial y} \frac{\partial y}{\partial \tau} + \frac{\partial X}{\partial z} \frac{\partial z}{\partial \tau}$$

From the transformations (3) given above, we have

$$\begin{aligned}
& \frac{\partial t}{\partial \tau} = \beta \\
(6) \quad & \frac{\partial x}{\partial \tau} = \beta \frac{v}{c} \\
& \frac{\partial y}{\partial \tau} = \frac{\partial z}{\partial \tau} = 0
\end{aligned}$$

Plugging (6) into (5) and dropping out the zero terms, we have

$$(7) \quad \frac{\partial X}{\partial \tau} = \beta \left[\frac{\partial X}{\partial t} + \frac{v}{c} \frac{\partial X}{\partial x} \right]$$

Now we substitute (1) and (2) into (7), multiply both sides by "1/c", and replace "y" and "z" with eta and zeta, to obtain

$$\frac{1}{c} \frac{\partial X}{\partial \tau} = \beta \left[\frac{\partial N}{\partial \eta} - \frac{\partial M}{\partial \zeta} - \frac{v}{c^2} \left(\frac{\partial Y}{\partial \eta} + \frac{\partial Z}{\partial \zeta} \right) \right]$$

which, with a little rearranging, is the first of the transformed equations Einstein gives,

$$\frac{1}{c} \frac{\partial X}{\partial \tau} = \frac{\partial}{\partial \eta} \left[\beta \left(N - \frac{v}{c} Y \right) \right] - \frac{\partial}{\partial \zeta} \left[\beta \left(M + \frac{v}{c} Z \right) \right]$$

except that, as usual, I messed up a factor of "c" someplace. (I much prefer to set c=1; then it doesn't matter if I blow a constant multiple of "c" somewhere...)

As I said, I think the rest of the them follow the same way but I haven't worked them all through in this detail.